

A Statistical Analysis of the Distribution of the Chloride Threshold with Relation to Steel-concrete Interface

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Abstract: A wide variation of chloride thresholds can be found in the literature. Possible causes for this variation, which were mentioned are: method of threshold determination, cement chemistry, and concrete microstructure. Regardless of the reasons for these variations, a probabilistic method can be used to ensure the durability of reinforced concrete structures for a specific period. A probabilistic method gives a threshold for design for given required confidence. A former research analyzed the micro-structure of concrete around steel rebar, by means of BSE automated image analysis, and the chloride threshold. The research found a statistical significant correlation between the maximal distance of steel from the closest concrete solid on the rebar perimeter and the chloride threshold. Theory of statistics of extreme values state, that the distribution of maxima data is bonded to be general extreme value distribution (GEVD). Re-analysis of the data from the abovementioned research found that as expected from the theory of statistics, the maximum steel-concrete distance distributed according to GEVD. Therefore, since the chloride threshold depends on the steel-concrete distance, its distribution is bonded to the GEVD. The analysis in this paper show that the received chloride threshold is GEVD as the theory predicted. From the theoretical point of view, GEVD may be the distribution of many other corrosion processes. The recognition of GEVD as the correct distribution for describing corrosion initiation in reinforced concrete (RC) structures, can enable more accurate planning for corrosion protection.

Keywords: Reinforced Concrete, Probabilistic Design, Chloride Threshold, Statistical Analysis, Corrosion

1. Introduction

When the chloride content near the rebar surface exceeds a certain limit, referred to as the chloride corrosion concentration limit (CCCL, also denoted as "threshold" in the followings), depassivation of the steel occurs and the steel is susceptible to corrosion; indeed, the corrosion hazard to the embedded reinforcement increases drastically above this level [1].

The chloride threshold for depassivation of steel embedded in concrete is an important parameter for the calculation of the time expected to pass before the initiation of corrosion of reinforced concrete. A change in the chloride threshold can have a significant effect on the lifetime of RC, as much as the transport properties of the concrete or the covercrete thickness. Thus, for example, according to LIFE-365 model [2], for a

specific case [3], a 20% increase in CCCL increases the time to initiation of corrosion by 28%, whereas a 20% reduction in the diffusion coefficient increases the time to initiation of corrosion by only 10%.

The chloride thresholds that can be found in the literature vary to an order of magnitude [3-4]. A revision of the range of the chloride threshold found to be in the range of 0.2% of total chloride to cement [5] to 8.34% of total chloride to cement in mortar [6]. When only the free chloride was measured, the range of the threshold is from 0.03% of cement [7] to 4% of cement [6]. Where Cl/OH is used for presenting the chloride threshold a range of 0.12 to 20 can be found in the literature [6]. These variations were attributed to several causes, including (a) the method of threshold determination [4], (b) cement chemistry [8], and (c) concrete microstructure [3, 9-10].

Regardless of the method used for chloride threshold

determination or the specific cement chemistry, chloride threshold variability remains high [4-3, 8-9]. It has been demonstrated that the chloride threshold is microstructure-dependent, and this dependence was reinforced by the localized corrosion mechanism of concentration polarization [3, 11-12]. Even though the microstructure is known to be a factor influencing the chloride threshold, it is currently an uncontrollable factor [13].

Nevertheless, a probabilistic approach may be applied to ensure the projected time to corrosion with pre-defined confidence. In other words, even if the exact time to corrosion cannot be calculated, because the values of variables controlling it are widely spread, the time for corrosion with exact confidence interval can be calculated [14]. For example, 1% probability of not having corrosion for 50 years, or having corrosion in less than 1% of the structure for 50 years. The variation of the covercrete, concrete effective diffusion coefficient, and chloride threshold have to be known, in order to build a complete probabilistic model for the duration to chloride induced corrosion initiation. The distribution of the covercrete was published in several papers [15]. Nevertheless, even though many papers report chloride threshold findings, there is shortness of data regarding chloride threshold distribution.

For using the probabilistic approach, information regarding the probability of having a chloride threshold which is equal to or greater than a specific value (cumulative distribution function - CDF) is needed. Creating this information by the use of parametric distribution, demands a large database of chloride thresholds, especially for the tail of lower probabilities, i.e. for having probability of 1% at least 100 specimens for chloride threshold determination are needed. Estimating the chloride threshold by using a known distribution, which is fitted to the data, allows finding the tail probabilities using less data.

Normal, log normal, and Weibull distributions have been used to estimate the distribution of the chloride threshold [4, 16-17]. The Weibull distribution was developed by Weibull for describing the distribution of processes outcome which are depended on the extreme of random parameter in the process. Later, the mathematic was improved by Weibull, Gumbel, Frechet, Leadbetter, Lindgren, Rootzen, and other mathematicians to create the generalized extreme value distribution (GEVD) and to establish its theory [18]. GEVD is a distribution that represents the extremes from groups of results, i.e. represents the extreme values taken from different sets of measurements that have the same distribution [19-18] and has been used to describe a variety of phenomenon, including pitting corrosion [20], concrete permeability [21], and reliability analysis of reinforced concrete.¹

The assumption that the chloride threshold is determined by the largest defect in the steel-concrete interface, which is being represented by the maximum steel-concrete distance [3], lead to that both maximum steel-concrete distance and

chloride threshold distributions are well represented by GEVD. The results reinforces the assumption that the variability of the interface is a major contribution to the chloride threshold. This implies that the GEVD should be used in order to determine the chloride threshold for design and surveillance.

This paper proposes using GEVD for the representation of the distribution of the chloride threshold. The GEVD is a consequence of the corrosion initiation, which is not all over the steel at once, but at the most vulnerable spot, as commonly observed, which where an extreme value is.

2. Methods

2.1. Mix Preparation

Sixteen different concrete mixes were produced with the following variables: (1) w/c ratios between 0.40 and 0.65; (2) water/powder ratios ranging from 0.91 to 1.36 at constant w/c ratios of either 0.45 or 0.52 where the powders includes all the particles smaller than 0.15 mm in the aggregates, cement, and limestone filler. The amount of powders was adjusted by adding fine limestone powder. The mixes were designed to yield different ITZ properties. The composition of the concrete mixes is given in Table 1. The concrete was mixed according to the following procedure: coarse aggregates were premixed with 70% of total water for 1 min. and allowed to absorb water for an additional 5min in rest. Fine aggregates, cement, powder, the rest of the water, and admixture were then added and mixed for an additional 3min. All mixes slumps were 80mm or higher. Other mix properties, which are irrelevant for the subject, are described in detail elsewhere [13].

Table 1. Concrete mix compositions per 1 m³.

Mix	Water	CEM I 52.5	Aggregates		Filer	HRWR
			Coarse	Fine		
W45	207	475	1384	287	0	4
W45C20	212	470	1384	184	94	5
W60	221	367	1393	355	0	0
W40	211	527	1360	249	0	5
W40B2	211	525	1356	249	0	5
W45C16	213	473	1373	204	76	5
W50	199	428	1396	339	0	2
W45C12	224	496	1374	187	60	5
W45C08	221	491	1348	223	39	4
W45C04	211	468	1360	299	19	5
W55	210	381	1352	400	0	2
W65	235	362	1390	335	0	0
W52C12	214	411	1378	279	50	4
W52C08	218	419	1378	300	34	4
W52C17	205	393	1386	325	68	6
W52C54	179	345	1163	496	208	6

2.2. Specimen Preparation

In order to reduce variability, which not arise from the steel-concrete microstructure, special attention was taken to assure uniform rebar preparation. All rebars were treated similarly prior to casting, as follows: immersion in H₃PO₄ 10% for two hours, washing and brushing under hot water, hot air

¹ Nevertheless, the Weibull distribution is included in the GEVD [18], so this do not reduce from validity of former works where Weibull distribution was used.

drying, immersion in saturated Ca(OH)₂ solution for 24 hours, drying, and positioning and fixing in molds.

To allow different types of ITZs to form, two types of molds were prepared for each concrete mix, with rebars in either horizontal or vertical orientation, with respect to cast direction. Specimen dimensions were 150 mm x 150 mm x 230 mm and net distance between rebars was 65 mm (Figure 1). Two duplicates were prepared for each rebar orientation. All specimens were cured in water at 20°C for one week and for an additional 21 days at 20°C, 100% RH.

After casting and curing, the exposed rebar tips were protected against corrosion to a depth of 20 mm into the concrete and wired for corrosion measurements. Scheme of rebar tip protection is shown in Figure 2.

Uniform concrete cover was achieved by sectioning the concrete at a distance of 10±2 mm from the surface of one of the rebars. This rebar was exposed to penetration of salt whereas the other rebar was used as reference. The side surface of the concrete close to the sectioned face was coated with room temperature vulcanization (RTV) silicone to ensure unidirectional penetration of the solution (Figure 1c).

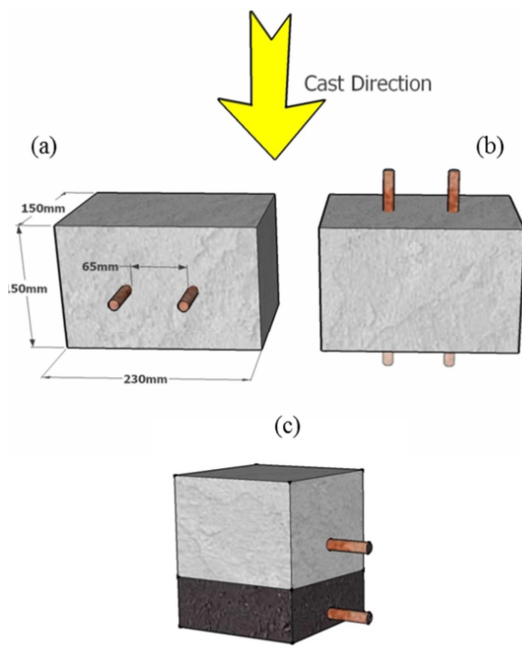


Figure 1. Dimensions of specimens for corrosion measurement. (a) Vertical rebar orientation. (b) Horizontal rebar orientation. (c) Specimen after sectioning of one edge to allow 10 mm between exposed face and tested rebar.

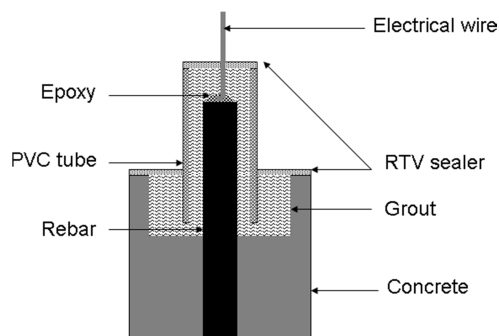


Figure 2. Rebar tip protection scheme.

2.3. Corrosion and Chloride Threshold Measurement

The sectioned face of the specimens was subjected to cycles consisting of two weeks immersion to a depth of 5 mm in a 6% (w/w) NaCl solution (Figure 3) followed by two weeks air-drying at 30°C, 30% RH. Corrosion initiation was monitored by measuring the potential difference between the upper and lower rebars of each concrete specimen. The lower rebar was closer to the chloride source and so corrosion was expected to initiate there. The upper rebar was used as an internal reference. Potential was measured against an Ag|AgCl half-cell for validation. A shift in potential of more than 100mV in one day was taken to indicate the breakdown of the passivation layer protecting the steel.

The potential shift indicating corrosion initiation was validated by analyzing several specimens using electrochemical impedance spectroscopy (EIS), which Ann and Song [23] considered to be the method that gives the most accurate information on corrosion. Good correlation was obtained between the two measuring methods, validating the potential shift results. It is important to mention that 100mV potential drop was found to be more accurate than ASTM G109 [17].

Upon detection of active corrosion, sixteen 4 mm diameter bores were drilled in each specimen, along a line parallel to the corroding rebar, 10 mm from the exposed surface. Powder from the bores was collected and dried. After drying, 2 g concrete powder was mixed with 40 ml distilled water, shaken for 2 hours, and allowed to settle for an additional 24 hours. Twenty ml of the supernatant fluid was acidified by adding 1 ml 1M HNO₃ and the chloride concentration of the solution was measured using an ion-selective electrode device. Chloride content was determined first as ‰ (1/1000) of concrete weight.

The moisture content in air dry and saturated were measured to calculate the chloride threshold as [Cl]. The moisture content was measured by weighing about 300 gr piece of the concrete, not including rebar, at the end of dry cycle, saturating the piece in water for two weeks, weighing again, oven drying in 105°C for 24 hours, and weighing again. Moisture content was calculated relative to the oven dry weight.

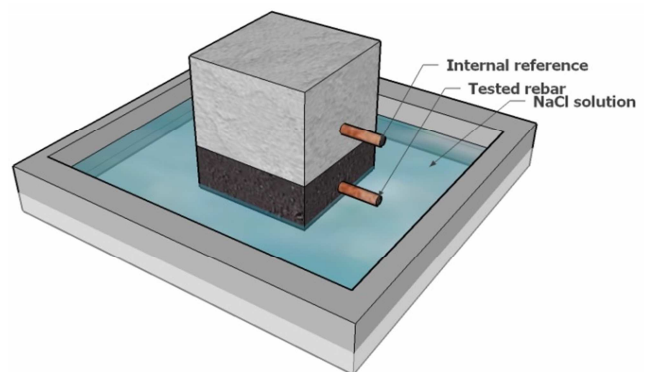


Figure 3. Corrosion test setup.

2.4. Microstructure Measurement

Back-scattered electron (BSE) images were taken from the areas all around the rebar of every mix and every rebar orientation. BSE images were analyzed automatically, as described by Kenny and Katz [24]. In short, two slices of 30mm×30mm×5mm each were prepared for each mix/orientation. The slice prepared perpendicular to the rebar longitudinal axis to show its cross-section and the surrounding concrete. After epoxy impregnation and polishing, the entire perimeter was scanned at x100 magnification to yield high-resolution image in which each pixel corresponds to ~0.65 μm . A total of ~1300 BSE images from 16 mixes and 2 rebar orientations were scanned and analyzed using the modified mean shift algorithm to properly cluster the pixels into the right phase (concrete, steel or void).

The steel-concrete distance, which is the distance from the rebar surface to the nearest concrete particle was calculated for each steel perimeter pixel, by using Euclidian distance on MATLAB image analysis toolbox. Note that steel-concrete distance represents the distance from the steel surface to the nearest concrete solid, including solid deposits on the steel surface.

2.5. Distribution Analysis

The distribution of chloride thresholds found in separated specimens, together with maximum steel-concrete distances, were fitted to different known distributions. Distribution fitting was done using MATLAB R2009b.

3. Results and Discussion

The distribution of the steel-concrete distance differs from commonly used distributions, and is most similar to exponential distribution, excluding its extremes (Figure 4). Ignoring the distribution of the steel-concrete distance in an image, or the maximum steel concrete distance that can be found around a rebar, have a generalized extreme value distribution (Figure 5 and Figure 6 respectively). A variable that is linearly related to another variable that is distributed according to GEVD, has a GEVD as well [19]. Hence, because the maximum steel-concrete distance around a rebar is expected to determine the chloride threshold [2], the chloride threshold itself is expected to have a generalized extreme value distribution.

The distribution of chloride thresholds that were found are shown in Table 2. The chloride threshold is best represented by the extreme value distribution (Figure 7 and Figure 8). This is most pronounced in the low cumulative probabilities range (Figure 9). The low cumulative probabilities are most important if the desired goal is to ensure the upper limit for corrosion risk.

For example, if the risk level is set to 5%, the chloride threshold that will be found by using normal distribution will be about 0.9 gr Cl-/kg concrete, while the thresholds found by generalized extreme value distribution and parametric

distribution are about 1.35 and 1.45 gr Cl-/kg concrete, respectively (Figure 9).

Because climate and different cementitious compositions may influence the chloride threshold, the threshold presented here should not be applied directly, because it was obtained for specific cement and environmental conditions.

The same statistics for analysis and to determine risk for corrosion initiation should be applied for other influencing factors, such as: covercrete thickness and concrete permeability. Since, in any real structure, covercrete thickness is varied, due to corrugation of the steel, flexure of the casting frames, and some time bad practice, the risk for corrosion is depended on the places where covercrete is minimal. The probability of such minimal thickness occurrence in specific building is described by GEVD. The permeability of the concrete is also variable, highly depended on local defects, like cracks and insufficient vibration. The critical, i.e. worst, permeability is the maximum one; hence, its occurrence is described by GEVD. The overall process for corrosion initiation depends on the maxima and minima of several properties, yielding GEVD for every corrosion initiation measurement.

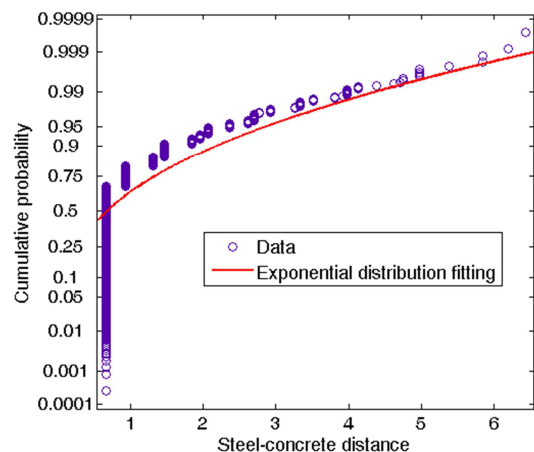


Figure 4. Probability plot for the distribution of the steel-concrete distance of one image, fit with an exponential distribution.

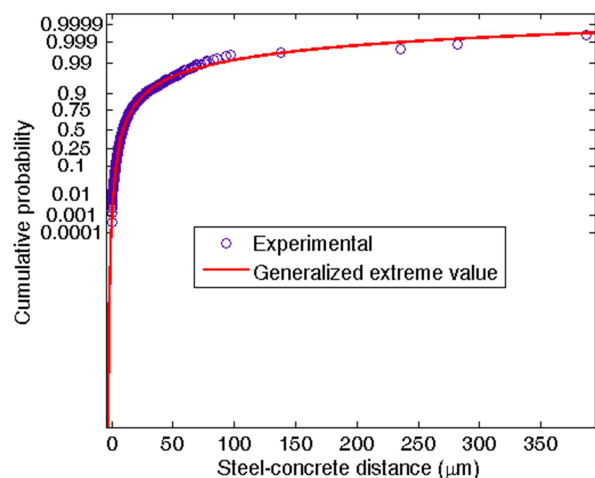


Figure 5. Probability plot for maximum steel-concrete distance in every image with GEVD fit.

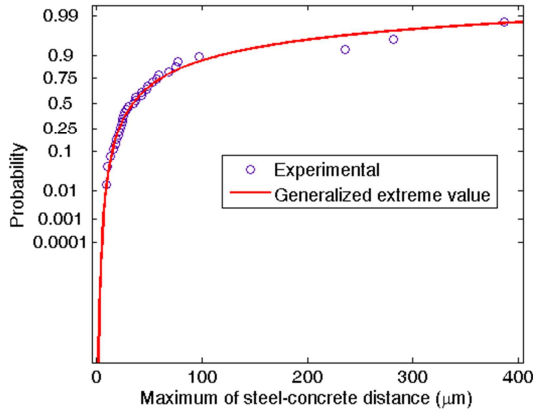


Figure 6. Probability plot for maximum steel-concrete distance around a rebar with GEVD fit.

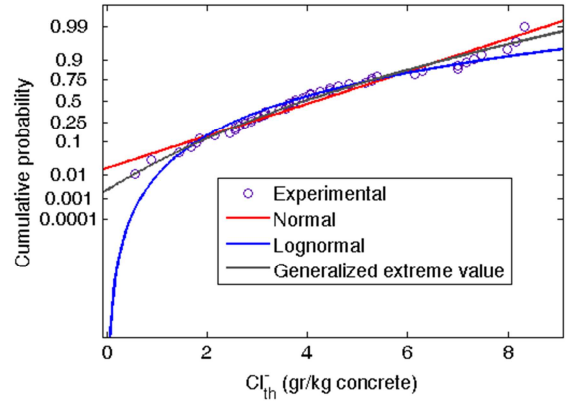


Figure 8. Probability plot for experimental value with some distributions fit to it.

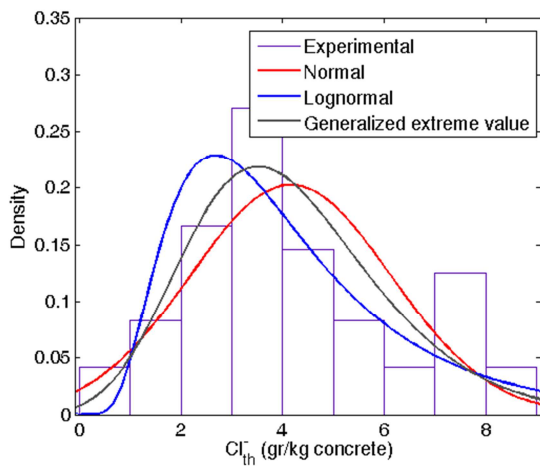


Figure 7. The experimental Cl_{th} distribution with some distributions fit to it.

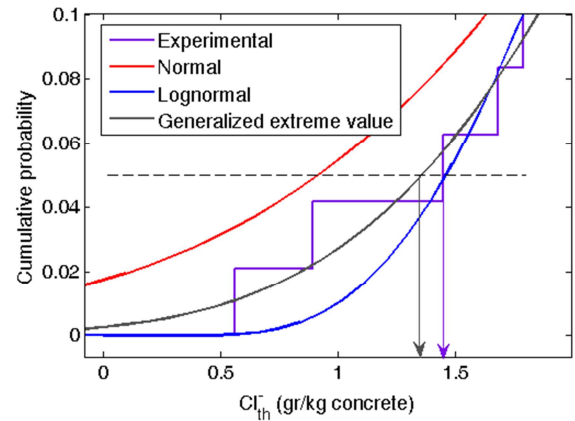


Figure 9. Cumulative probability of the chloride threshold and distributions fitting at low probabilities.

Table 2. Chloride threshold measured (free chloride as % of concrete weight) and calculated to other common threshold representations.

Mix	Orientation	Repetition	% concrete (w/w)	% of cement (w/w)	[Cl ⁻] (molar)	
W40	H	1	4.44	1.982	1.666	1.915
W40	H	2	7.16	3.197	2.686	3.088
W40B2	H	1	2.46	1.098	0.944	1.089
W40B2	H	2	3.91	1.746	1.500	1.730
W45	H	1	2.56	1.272	1.013	1.207
W45	H	2	0.56	0.278	0.222	0.264
W45C04	H	1	5.39	2.718	2.114	2.462
W45C04	H	2	7.31	3.686	2.867	3.339
W45C08	H	1	1.79	0.848	0.644	0.776
W45C08	H	1	2.65	1.256	0.954	1.150
W45C12	H	2	4.07	1.925	1.374	1.566
W45C16	H	1	3.16	1.566	1.186	1.347
W45C16	H	1	7.47	3.701	2.804	3.184
W45C16	H	2	5.29	2.621	1.986	2.255
W45C20	H	1	1.68	0.840	0.646	0.756
W45C20	H	2	5.28	2.639	2.032	2.377
W50	H	1	0.75	0.414	0.281	0.309
W50	H	2	0.2	0.110	0.075	0.082
W52C08	H	1	2.88	1.618	1.048	1.206
W52C08	H	2	2.88	1.618	1.048	1.206
W52C12	H	1	3.73	2.120	1.398	1.697
W52C12	H	2	0.89	0.506	0.334	0.405
W52C17	H	1	0.31	0.188	0.124	0.141
W52C17	H	2	0.36	0.218	0.144	0.164

Mix	Orientation	Repetition	% concrete (w/w)	% of cement (w/w)	[Cl ⁻] (molar)	
W52C54	H	2	3.64	2.533	2.084	2.256
W55	H	1	1.45	0.892	0.558	0.645
W55	H	2	2.76	1.699	1.063	1.227
W60	H	1	3.03	1.928	1.077	1.230
W60	H	2	4.62	2.939	1.643	1.875
W65	H	1	7.8	5.003	2.646	2.885
W40	V	1	3.56	1.590	1.336	1.535
W40	V	2	2.56	1.143	0.960	1.104
W40B2	V	1	2.89	1.290	1.108	1.279
W40B2	V	2	3.15	1.406	1.208	1.394
W45	V	1	6.86	3.408	2.716	3.236
W45	V	2	0.31	0.154	0.123	0.146
W45C04	V	2	3.64	1.836	1.428	1.663
W45C04	V	2	3.97	2.002	1.557	1.813
W45C04	V	2	4.84	2.441	1.898	2.211
W45C08	V	1	4.07	1.929	1.465	1.765
W45C12	V	1	5.06	2.393	1.708	1.947
W45C12	V	2	3.44	1.627	1.161	1.323
W45C16	V	1	6.29	3.117	2.361	2.681
W45C16	V	2	3.59	1.779	1.348	1.530
W45C20	V	1	4.44	2.219	1.708	1.999
W45C20	V	2	4.25	2.124	1.635	1.913
W50	V	1	3.44	1.900	1.290	1.417
W50	V	2	3.75	2.071	1.406	1.545
W52C08	V	1	1.86	1.045	0.677	0.779
W52C08	V	2	7	3.932	2.547	2.932
W52C12	V	1	5.16	2.933	1.934	2.348
W52C12	V	2	5.16	2.933	1.934	2.348
W52C17	V	1	3.14	1.902	1.253	1.431
W52C17	V	2	6.14	3.719	2.450	2.799
W52C54	V	2	2.16	1.503	1.237	1.339
W55	V	1	8.33	5.127	3.207	3.703
W55	V	2	7	4.308	2.695	3.112
W60	V	2	1.42	0.903	0.505	0.576
W60	V	2	2.91	1.851	1.035	1.181
W65	V	1	7.98	5.118	2.707	2.952
W65	V	2	8.15	5.228	2.765	3.014

4. Conclusions

The results presented in this paper may have a wider application than durability of reinforced concrete only. Many corrosion initiation processes may behave similarly, therefore the below conclusions may be adopted.

- i. The distribution of chloride thresholds in concrete, which can be found in field or laboratory, should be interpreted as generalized extreme values.
- ii. Adapting GEVD distribution allows more accurate assessment of the risk of corrosion. This can be used in
 - a. building surveys
 - b. assessing corrosion risk in the design stage
 - c. establishment of standards

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